

check point - 5 - C

1. list the common factors of each of the following set of numbers and hence find their HCF

$$(a) \quad 10 = 1, 2, 5, 10$$

$$15 = 1, 3, 5, 15$$

$$C.F = 1, 5$$

$$HCF = 5$$

$$(b) \quad 70 = 1, 2, 5, 7, 10, 35, 70$$

$$120 = 1, 2, 3, 4, 5, 6, 8, 10, 12, 15, 20, 24, 30, 40, 60, 120$$

$$C.F = 1, 2, 5, 10$$

$$HCF = 10$$

$$(c) 42 = 1, 2, 3, 6, 7, 14, 21, 42$$

$$64 = 1, 2, 4, 8, 16, 32, 64$$

$$C.F. = 1, 2$$

$$HCF = 2$$

$$(d) 100 = 1, 2, 4, 5, 10, 20, 25, 50, 100$$

x

$$120 = 1, 2, 3, 4, 5, 6, 8, 10, 12, 15, 20, 24, 30, 40, 60, 120$$

$$20 = 1, 2, 4, 5, 10, 20$$

$$C.F. = 1, 2, 4, 5, 10, 20$$

$$H.C.F. = 20$$

$$(e) 256 = 1, 2, 4, 8, 16, 32, 64, 128, 256$$

~~128~~

$$132 = 1, 2, 3, 4, 6, 11, 22, 33, 44, 66, 132$$

$$64 = 1, 2, 4, 8, 16, 32, 64$$

$$C.F. = 1, 2, 4$$

$$H.C.F. = 4$$

~~Q.2~~

$$(f) \quad 500 = 1, 2, 4, 5, 10, 20, 25, 50, 100, 125, 250, 500$$

$$625 = 1, 5, 25, 125, 625$$

$$225 = 1, 3, 5, 9, 15, 25, 45, 75, 225$$

$$C.F = 1, 5, 25$$

$$H.C.F = 25$$

$$(g) \quad 200 = 1, 2, 4, 5, 8, 10, 20, 25, 40, 50, 100, 200$$

$$400 = 1, 2, 4, 5, 8, 10, 16, 20, 25, 40, 50, 80, 100, 200, 400$$

$$650 = 200, 400$$

$$650 = 1, 2, 5, 10, 13, 25, 26, 50, 65, 130, 325, 650$$

$$C.F = 1, 2, 5, 10, 25, 50$$

$$H.C.F = 50$$

Ex: 5(c)

Q.2 Find HCF by prime factorisation method

(a) 32, 40

$$\begin{array}{r|l}
 2 & 32 \\
 2 & 16 \\
 2 & 8 \\
 2 & 4 \\
 2 & 2 \\
 & 1
 \end{array}$$

$$\begin{array}{r|l}
 2 & 40 \\
 2 & 20 \\
 2 & 10 \\
 5 & 5 \\
 & 1
 \end{array}$$

$$\begin{aligned}
 32 &= (2) \times (2) \times (2) \times 2 \times 2 \\
 40 &= (2) \times (2) \times (2) \times 5
 \end{aligned}$$

$$HCF = 2 \times 2 \times 2 = 8$$

(b) 50, 80

$$\begin{array}{r|l}
 2 & 50 \\
 5 & 25 \\
 5 & 5 \\
 & 1
 \end{array}$$

$$\begin{array}{r|l}
 2 & 80 \\
 2 & 40 \\
 2 & 20 \\
 2 & 10 \\
 5 & 5 \\
 & 1
 \end{array}$$

$$\begin{aligned}
 50 &= (2) \times 5 \times 5 \\
 80 &= 2 \times 2 \times 2 \times 2 \times 5
 \end{aligned}$$

$$HCF = 2 \times 5 = 10$$

(c) 130, 150

$$\begin{array}{r|l}
 2 & 130 \\
 5 & 65 \\
 13 & 13 \\
 & 1
 \end{array}$$

$$\begin{array}{r|l}
 2 & 150 \\
 3 & 75 \\
 5 & 25 \\
 5 & 5 \\
 & 1
 \end{array}$$

$$\begin{aligned}
 130 &= (2) \times (5) \times 13 \\
 150 &= (2) \times 3 \times (5) \times 5
 \end{aligned}$$

$$HCF = 2 \times 5 = 10$$

(d) 132, 140, 250

$\begin{array}{r l} 2 & 132 \\ \hline 2 & 66 \\ 3 & 33 \\ 11 & 11 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 2 & 140 \\ \hline 2 & 70 \\ 5 & 35 \\ 7 & 7 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 2 & 250 \\ \hline 5 & 125 \\ 5 & 25 \\ 5 & 5 \\ \hline & 1 \end{array}$	$132 - (2) \times 2 \times 3 \times 11$ $140 - (2) \times 2 \times 5 \times 7$ $250 - (2) \times 5 \times 5 \times 5$
			HCF = 2

(e) 165, 285, 225

$\begin{array}{r l} 3 & 165 \\ \hline 5 & 55 \\ 11 & 11 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 3 & 285 \\ \hline 5 & 95 \\ 19 & 19 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 3 & 225 \\ \hline 3 & 75 \\ 5 & 25 \\ 5 & 5 \\ \hline & 1 \end{array}$	$165 - (3) \times (5) \times 11$ $285 - (3) \times (5) \times 19$ $225 - (3) \times (3) \times (5) \times 5$
			HCF = $3 \times 5 = 15$

(f) 90, 450, 1875

$\begin{array}{r l} 2 & 90 \\ \hline 3 & 45 \\ 3 & 15 \\ 5 & 5 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 2 & 450 \\ \hline 3 & 225 \\ 3 & 75 \\ 5 & 25 \\ 5 & 5 \\ \hline & 1 \end{array}$	$\begin{array}{r l} 3 & 1875 \\ \hline 5 & 625 \\ 5 & 125 \\ 5 & 25 \\ 5 & 5 \\ \hline & 1 \end{array}$	$90 - 2 \times (3) \times 3 \times 5$ $450 - 2 \times (3) \times 3 \times 5 \times 5$ $1875 - (3) \times 5 \times 5 \times 5 \times 5$
			HCF = $3 \times 5 = 15$

(9) 500, 750, 1000

<u>2</u> 500	<u>2</u> 750	<u>2</u> 1000
<u>2</u> 250	<u>3</u> 375	<u>2</u> 500
<u>5</u> 125	<u>5</u> 125	<u>2</u> 250
<u>5</u> 25	<u>5</u> 25	<u>5</u> 125
<u>5</u> 5	<u>5</u> 5	<u>5</u> 25
1	1	<u>5</u> 5
		1

$$\begin{aligned}
 500 &= (2) \times 2 \times (5) \times (5) \times (5) \\
 750 &= 2 \times 3 \times 5 \times 5 \times 5 \\
 1000 &= 2 \times 2 \times 2 \times 5 \times 5 \times 5
 \end{aligned}$$

$$\begin{aligned}
 \text{HCF} &= 2 \times 5 \times 5 \times 5 \\
 &= 250
 \end{aligned}$$

Checkpoint 5C.

Q.3 Find the HCF by long division method.

(a)

$$\begin{array}{r}
 18 \overline{) 90} \quad (5 \\
 \underline{-90} \\
 00
 \end{array}$$

HCF = 18

(b)

$$\begin{array}{r}
 92 \overline{) 132} \quad (1 \\
 \underline{-92} \\
 40 \overline{) 92} \quad (2 \\
 \underline{-80} \\
 12 \overline{) 40} \quad (3 \\
 \underline{-36} \\
 04 \overline{) 12} \quad (3 \\
 \underline{-12} \\
 00
 \end{array}$$

HCF = 4

(c)

$$\begin{array}{r}
 330 \overline{) 13314} \\
 \underline{- 1320} \\
 11 \overline{) 330} (30 \\
 \underline{- 330} \\
 000
 \end{array}$$

$$\text{HCF} = \boxed{11}$$

(d)

$$\begin{array}{r}
 132 \overline{) 1100} (8 \\
 \underline{- 1056} \\
 44 \overline{) 132} (3 \\
 \underline{- 132} \\
 000
 \end{array}$$

$$\text{Initial HCF} = \boxed{44}$$

$$\begin{array}{r}
 44 \overline{) 88} (2 \\
 \underline{- 88} \\
 00
 \end{array}$$

$$\text{Final HCF} = \boxed{44}$$

$$(c) \quad 52 \overline{) 197} \begin{matrix} 3 \\ 156 \end{matrix}$$

$$41 \overline{) 52} \begin{matrix} 1 \\ -41 \end{matrix}$$

$$11 \overline{) 41} \begin{matrix} 3 \\ -33 \end{matrix}$$

$$8 \overline{) 11} \begin{matrix} 1 \\ -8 \end{matrix}$$

$$3 \overline{) 8} \begin{matrix} 2 \\ -6 \end{matrix}$$

$$2 \overline{) 3} \begin{matrix} 1 \\ -2 \end{matrix}$$

$$\text{HCF} \quad 1 \overline{) 2} \begin{matrix} 2 \\ -2 \end{matrix}$$

HCF of 197 and 52 is 1

$$\text{HCF} \quad 1 \overline{) 9} \begin{matrix} 9 \\ -9 \end{matrix}$$

$\therefore$ HCF of 197, 52 and 9 is 1

$$(f) \quad 1 \overline{) 2} (2$$

$$\underline{- 2}$$

$$0$$

Initial

$$HCF = \boxed{1}$$

$$1 \overline{) 3} (3$$

$$\underline{- 3}$$

$$0$$

$$\text{Final HCF} = \boxed{1}$$

(g)

$$1 \overline{) 275} (1$$

$$\underline{- 275}$$

$$75 \overline{) 275} (3$$

$$\underline{- 225}$$

$$50 \overline{) 75} (1$$

$$\underline{- 50}$$

$$25 \overline{) 50} (2$$

$$\underline{- 50}$$

$$00$$

$$\text{Initial HCF} = 25$$

$$25 \overline{) 625} (25$$

$$\underline{- 625}$$

$$000$$

$$\text{Final HCF} = \boxed{25}$$

Q4. Find the greatest number that exactly divides 155 and 215.

$$155 \overline{) 2115} \quad 13$$

$$\underline{- 2015}$$

$$100 \overline{) 155} \quad 1$$

$$\underline{- 100}$$

$$55 \overline{) 100} \quad 1$$

$$\underline{- 55}$$

$$45 \overline{) 55} \quad 1$$

$$\underline{- 45}$$

$$10 \overline{) 45} \quad 4$$

$$\underline{- 40}$$

$$5 \overline{) 10} \quad 2$$

$$\underline{- 10}$$

$$0$$

$$\text{HCF} = 5$$

∴ The greatest number that exactly divides 155 & 215 is 5.

Q.5 If a number leaves remainder 2, then after subtracting 2 from each number, that number should divide them exactly.

$$\text{HCF of } (194-2) = \boxed{192} \text{ and } (546-2) = \boxed{544}$$

$$192 \overline{) 544} 2$$

$$\underline{- 384}$$

$$160 \overline{) 192} 1$$

$$\underline{- 160}$$

$$\text{HCF} \rightarrow \boxed{32} \overline{) 160} 5$$

$$\underline{- 160}$$

$$0$$